



Cornell University
Office of Statistical Consulting

Colleges of Human Ecology and Agriculture and Life Sciences
 Division of Nutritional Sciences

StatNews #01: Sparse Contingency Tables

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With data obtained from both laboratory experiments and surveys, one is often confronted with frequency (or contingency) tables representing the occurrences of combinations of two categorical variables. A next step often involves testing the hypothesis of no association between the row variable and the column variable or testing the equality of proportions.

For example, one might be interested in the number of fish of different species caught in three different lakes.

| | SALMON | TROUT | BASS |
|-------------|--------|-------|------|
| KEUKA LAKE | 0 | 2 | 0 |
| SENECA LAKE | 0 | 4 | 0 |
| CAYUGA LAKE | 13 | 5 | 1 |

When requesting a Pearson chi-square test with such a table, to test the independence of the lake and bacteria variables, you might have been disconcerted by the warning message: " 77.8% of the cells have expected counts less than 5. Chi-square may not be a valid test."

The reason for this message is that asymptotic methods, which invoke the Central Limit Theorem, are not reliable when the data are sparse, skewed or heavily tied. Previously a solution to this problem was found by collapsing categories of variables or by transforming the problematic variables. These methods are not ideal since they entail a loss of information that in some cases is of major interest.

Now we can rely on exact methods which will calculate p-values by constructing a reference set of all possible outcomes in which the exact null probability of each outcome is known. Then summing up the probabilities of those outcomes in the reference set that are at least as extreme as the one observed, will produce the exact p-value.

In the example above the asymptotic p-value equals 0.0244 whereas the exact method yields a p-value equal to 0.0861. The difference in the two values might in some cases lead you to quite different interpretations. A few exact tests may be implemented in standard statistical packages. In addition, specialized software is available to implement exact p-values and confidence intervals for a wide range of tests. StatXact is the best known package. It is very easy to use and allows you to obtain your desired answer in less than 5 minutes.

Along the same line we also have LogXact which will present, besides maximum likelihood estimation of the parameters in logistic regression, exact inference which will yield exact p-values and confidence intervals for the effect of covariates.

These packages are available for your use in the Office of Statistical Consulting. If you experience a need for these methods, please contact Francoise Vermeylen.

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